

Name: _____

KEY

Physics – Conservation of Momentum: Collisions Practice

Types:

- Total momentum before = Total momentum after $(P_{Ai} + P_{Bi} = P_{Af} + P_{Bf})$
- Momentum is a vector; be sure you give each term the correct sign
- If the two objects stick together, they have the same final velocity

1) Two freight cars, each with a mass of 3.0×10^5 kg, collide. One was initially moving to the right at 2.2 m/s; the other was at rest. They stick together. What is their final velocity (magnitude and direction)?

$$\text{MOMENTUM BEFORE} = \text{MOMENTUM AFTER}$$

$$(3.0 \times 10^5 \text{ kg})(+2.2 \text{ m/s}) + \emptyset = (3 \times 10^5 \text{ kg} + 3 \times 10^5 \text{ kg}) \vec{v}$$

$$\boxed{+1.1 \text{ m/s} = \vec{v}}$$

2) A 0.105-kg hockey puck moving at +24 m/s is caught and held by a 75-kg goalie initially at rest. If the surface is frictionless, what is the velocity of the goalie and puck after the collision?

$$\vec{P}_{\text{Puck}_i} + \emptyset = \vec{P}_{\text{Goalie} + \text{Puck}_f}$$

$$(0.105 \text{ kg})(+24 \text{ m/s}) = (75 \text{ kg} + 0.105 \text{ kg}) \vec{v}$$

$$\boxed{+0.0336 \text{ m/s} = \vec{v}}$$

3) A 0.035-kg bullet strikes a 5.00-kg stationary wooden block sitting on a frictionless surface. The bullet embeds itself in the block. The block and bullet slide off together at +8.6 m/s. What was the original velocity of the bullet?

$$P_{\text{Bullet}_i} + \emptyset = P_{\text{Bullet} + \text{Block}_f}$$

$$(0.035 \text{ kg})(\vec{v}_i) = (5.035 \text{ kg})(+8.6 \text{ m/s})$$

$$\boxed{\vec{v}_i = 1240 \text{ m/s}}$$

4) Glider A ($m = 0.355 \text{ kg}$) moves along a frictionless air track with a velocity of $+0.095 \text{ m/s}$. It collides with glider B ($m = 0.710 \text{ kg}$), which has a velocity of $+0.045 \text{ m/s}$. After the collision glider A is moving at $+0.035 \text{ m/s}$. What is the velocity of glider B after the collision?

$$\vec{P}_{A_i} + \vec{P}_{B_i} = \vec{P}_{A_f} + \vec{P}_{B_f}$$

$$(0.355 \text{ kg})(+0.095 \text{ m/s}) + (0.710 \text{ kg})(+0.045 \text{ m/s}) = (0.355 \text{ kg})(+0.035 \text{ m/s}) + (0.710 \text{ kg})\vec{v}$$

$$\boxed{+0.075 \text{ m/s} = \vec{v}}$$

5) A 0.50-kg ball ^A traveling at $+6.0 \text{ m/s}$ collides head-on with a 1.00-kg ball ^B moving at -12.0 m/s . The 0.50-kg ball bounces backwards at -14 m/s after the collision. What is the velocity of the second ball after the collision?

$$\vec{P}_{A_i} + \vec{P}_{B_i} = \vec{P}_{A_f} + \vec{P}_{B_f}$$

$$(0.50 \text{ kg})(+6.0 \text{ m/s}) + (1.00 \text{ kg})(-12.0 \text{ m/s}) = (0.50 \text{ kg})(-14 \text{ m/s}) + (1.00 \text{ kg})\vec{v}$$

$$\boxed{-2 \text{ m/s} = \vec{v}}$$

6) A 5.00-g ^{0.005 kg} bullet is fired with a velocity of $+100 \text{ m/s}$ toward a 10.0-kg stationary block resting on a horizontal surface. The coefficient of kinetic friction between the block and surface is 0.24 .

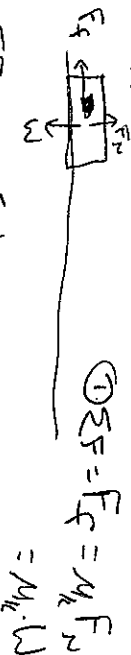
(a) If the bullet embeds itself in the block, determine the velocity of the bullet/block after the collision.

$$\vec{P}_{\text{bullet}_i} + \vec{P}_{\text{block}_i} = \vec{P}_{\text{bullet+block}_f}$$

$$(0.005 \text{ kg})(+100 \text{ m/s}) = (10.005 \text{ kg})\vec{v}_f$$

$$\boxed{+0.0500 \text{ m/s} = \vec{v}_f}$$

(b) How far does the block slide on the horizontal surface before coming to rest?



$$\sum F = F_f = \mu_k F_N = \mu_k W$$

$$kE_f = \frac{1}{2} m v^2 = 0.0125 \text{ J}$$

$$W_{\text{friction}} = \Delta kE = -0.0125 \text{ J}$$

$$-0.0125 \text{ J} = (F_f \cos \theta) s$$

$$\frac{-0.0125 \text{ J}}{(23.5 \text{ N} \cos 180^\circ)} = s = \boxed{5.32 \times 10^{-4} \text{ m}}$$

$$\textcircled{2} \frac{\sum F}{a} = \frac{23.5 \text{ N}}{10.005 \text{ kg}} = 2.35 \text{ m/s}^2 = 23.5 \text{ N}$$

$$\textcircled{3} v^2 = v_0^2 + 2ax$$

$$\boxed{5.32 \times 10^{-4} \text{ m} = x}$$

$$v_0 = +0.05 \text{ m/s}$$

$$v = 0$$

$$a = -2.35 \text{ m/s}^2$$

$$x = ?$$

Name: KEY
 Physics – Conservation of Momentum: Explosions Practice

Tips:

- Total momentum before = Total momentum after ($p_{Ai} + p_{Bi} = p_{Af} + p_{Bf}$)
- Momentum is a vector; be sure you give each term the correct sign
- In explosions, if the two objects start together at rest, the total momentum before equals zero; therefore, the final momentum of one must be equal and opposite to the final momentum of the other

1) A 50-kg woman stands on a 10-kg cart, both initially at rest. She jumps off the front of the cart, achieving a velocity of +7.0 m/s. What is the velocity of the cart after the woman jumps off?

Momentum Before = Momentum After

$$0 = \vec{p}_{\text{woman}} + \vec{p}_{\text{cart}}$$

$$0 = (50 \text{ kg})(+7 \text{ m/s}) + (10 \text{ kg})\vec{v}_{\text{cart}}$$

$$\boxed{-35 \text{ m/s} = \vec{v}_{\text{cart}}}$$

2) Two students on roller skates stand face-to-face and push off of each other. One student has a mass of 90 kg; the other has a mass of 60 kg. The more massive student has a velocity of -2.5 m/s after they push off. Determine the velocity of the less massive student.

$$0 = \vec{p}_1 + \vec{p}_2$$

$$= (90 \text{ kg})(-2.5 \text{ m/s}) + (60 \text{ kg})\vec{v}$$

$$\boxed{+3.75 \text{ m/s} = \vec{v}}$$

3) A 7.5×10^4 -kg space probe sits motionless in space (far from any star or planet). It fires its rocket, propelling 1500 kg of fuel at a speed of 3200 m/s into space. What is the speed of the probe after firing the rocket?

$$0 = \vec{p}_{\text{probe}} + \vec{p}_{\text{fuel}}$$

$$= (7.5 \times 10^4 \text{ kg})\vec{v}_{\text{probe}} + (1500 \text{ kg})(3200 \text{ m/s})$$

$$\boxed{-64 \text{ m/s} = \vec{v}_{\text{probe}}}$$

(Negative implies the probe is traveling in the opposite dir. of the expelled fuel)

4) A 75-kg student stands motionless on a frozen lake (frictionless surface) carrying nothing but his 2.5-kg Physics book. He throws the book east with a velocity of 18 m/s. What is the magnitude and direction of the student's velocity after throwing the book?

$$0 = \vec{p}_{\text{student}} + \vec{p}_{\text{book}} \quad \begin{matrix} \leftarrow \vec{w} \\ \rightarrow \vec{e} \end{matrix}$$

$$= (75 \text{ kg})v + (2.5 \text{ kg})(+18 \text{ m/s})$$

$$-0.6 \text{ m/s} = v$$

$$0.6 \text{ m/s west}$$

5) A two-stage rocket moves in space at a constant velocity of +4900 m/s. The two stages are then separated by a small explosive charge placed between them. Immediately after the explosion the velocity of the 1200-kg upper stage is +5700 m/s. What is the velocity of the 2400-kg lower stage after the explosion?

$$\vec{p}_i = \vec{p}_{\text{upper } \uparrow} + \vec{p}_{\text{lower } \uparrow}$$

$$(3600 \text{ kg})(+4900 \text{ m/s}) = (1200 \text{ kg})(+5700 \text{ m/s}) + (2400 \text{ kg})\vec{v}$$

$$+4500 \text{ m/s} = \vec{v}$$